

Research Agenda



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Motivation

Proposition 2 (expectation value of waiting time times tunnel rate) *For every PDF $f(x)$ in means of definition (0.1) the inequality*

$$\langle x \rangle \left\langle \frac{1}{x} \right\rangle \geq 1 \quad (0.10)$$

is valid.

26th of February 2011



I. POSITIVITY OF FANO FACTOR PARAMETERS

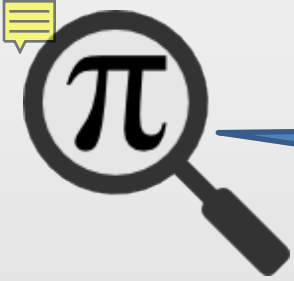
For every convex function $f(x)$, we have according to the Jensen inequality

$$f(\langle x \rangle) \leq \langle f(x) \rangle \quad (1)$$

That means that

$$\langle x \rangle^{-k} \leq \langle x^{-k} \rangle. \quad (2)$$

Especially $k = 1$ leads to the fact that $\alpha \geq 0$. 28th of March



Solution: Use a data-driven approach

Question

Proposition 2 (expectation value of waiting time t in means of definition (0.1) the inequality

$$\langle x \rangle \langle \frac{1}{x} \rangle \geq 1$$

is valid.

Goal: Find well established concepts related to a mathematical problem.

26th of February 2011



18.03.-26.03.2011

I. POSITIVITY OF FANO FACTOR PARAMETERS

Problem: The current search is slow, expensive and not deterministic

$$\langle x \rangle^{-k} \leq \langle x^{-k} \rangle. \tag{2}$$

Especially $k = 1$ leads to the fact that $\alpha \geq 0$. 28th of March



Example 1: $\frac{1}{\langle x \rangle} \leq \left\langle \frac{1}{x} \right\rangle$

1. Different forms e.g.

$$\langle x \rangle \left\langle \frac{1}{x} \right\rangle \geq 1$$

2. Different notations e.g.

$$\int_X f(x) x dx = \langle x \rangle$$

3. Exact match seldom

4. Ambiguity in syntax e.g.

$$E\Psi = \hat{H}\Psi$$

5. no TeX-function mean

```
\frac 1 \mean ?x \le  
\mean \frac 1 ?x$
```

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<apply>  
<leq/>  
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<cn type="integer">1</cn>  
<apply>  
<mean/>  
<qvar>x</qvar></apply></apply>  
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<divide>  
<cn type="integer">1</cn>  
<qvar>x</qvar></apply></apply>...
```

NTCIR-11
Math-2
WMC-D1



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3. **Exact match seldom**

~~4. Ambiguity in syntax e.g.~~

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DRMF

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NTCIR-11
Math-2
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Result 1: $\varphi(\mathbb{E}[X]) \leq \mathbb{E}[\varphi(X)]$

```
 $?f[type=function] \mean ?x \le  
\mean ?f[type=function] ?x $
```

```
<apply>
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```
<leq/>
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<apply>
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<qvar type="function">f</qvar>
```

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<apply>
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<mean/>
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<qvar>x</qvar></apply></apply>
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```
<apply>
```

```
<leq/>
```

```
<apply>
```

$\frac{1}{\mathbb{E}[X]} \leq \mathbb{E}\left[\frac{1}{X}\right]$

Not trivial

```
<apply>
```

```
<mean/>
```

```
<apply>
```

```
<divide>
```

```
<cn type="integer">1</cn>
```

```
<qvar>x</qvar></apply></apply>...
```



Solution 1 inexact matches

- Refined query:

```
$_\superconceptOf[  
  orderby = editdistance ]{  
  \frac 1 \mean ?x \le  
  \mean \frac 1 ?x  
}$
```

- Computational complexity
- Restriction of the search space
- Check most likely solutions at first



Tasks inexact matches

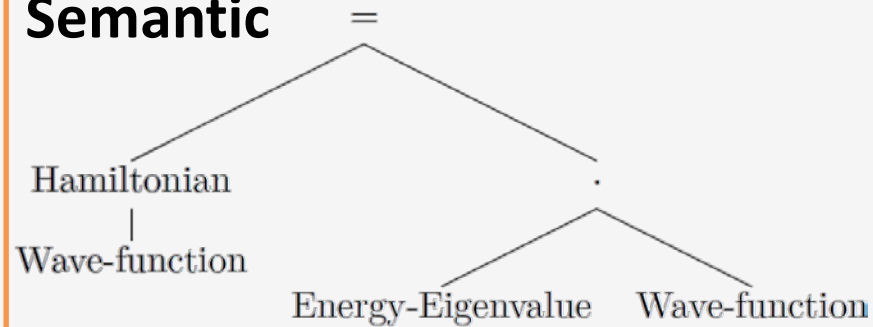
```
 $\superconceptOf[ orderby = editdistance ]{  
   \frac 1 \mean ?x \le  
   \mean \frac 1 ?x  
 }$
```

1. Related work (applicable theorem search and citation recommender)
2. Identification of the key indicators for relatedness
3. Development of methods to calculate relatedness
4. Implementation of a prototype
5. Automated evaluation and comparison of the proposed methods

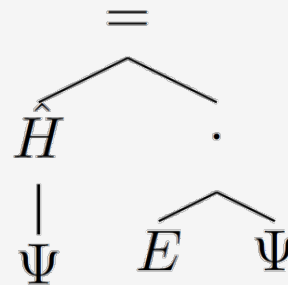


Topic Overview: Levels of Abstraction

Semantic



Content

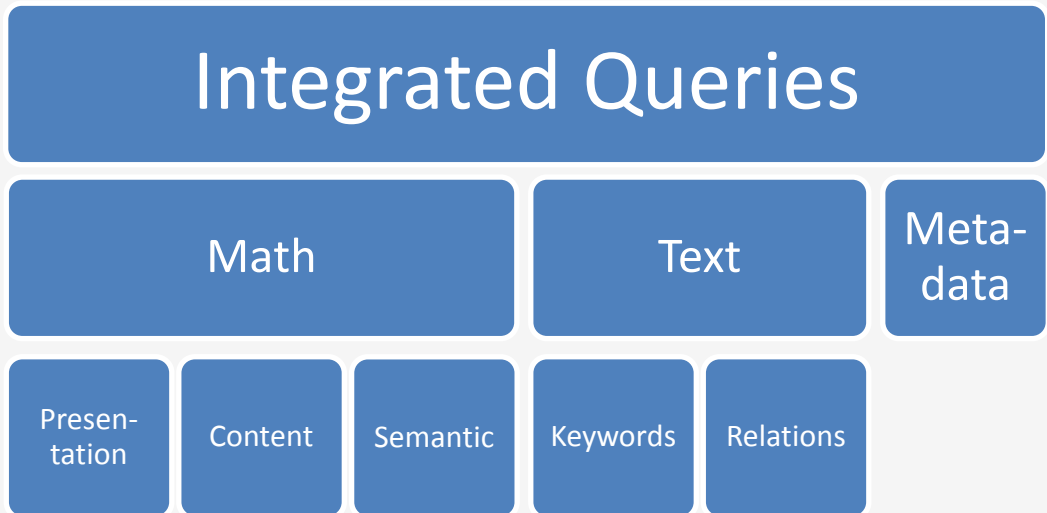
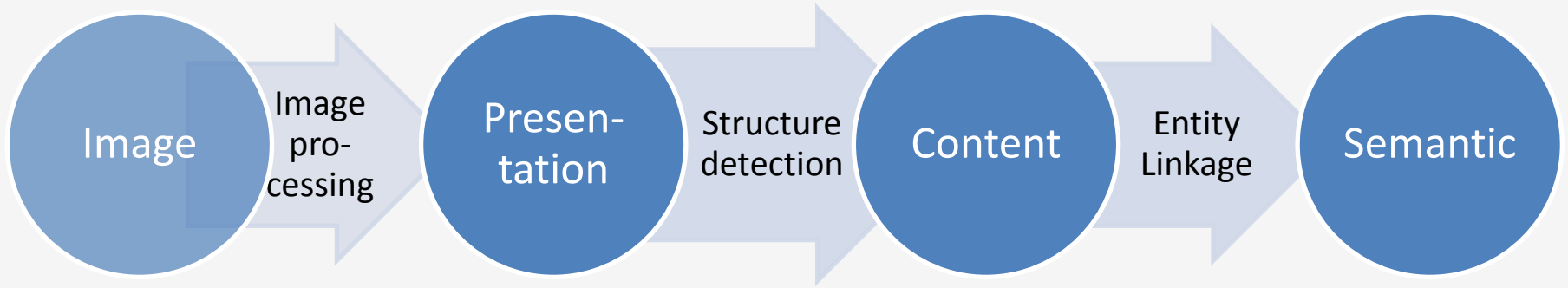


Presentation

$$\hat{H}\Psi = E\Psi$$

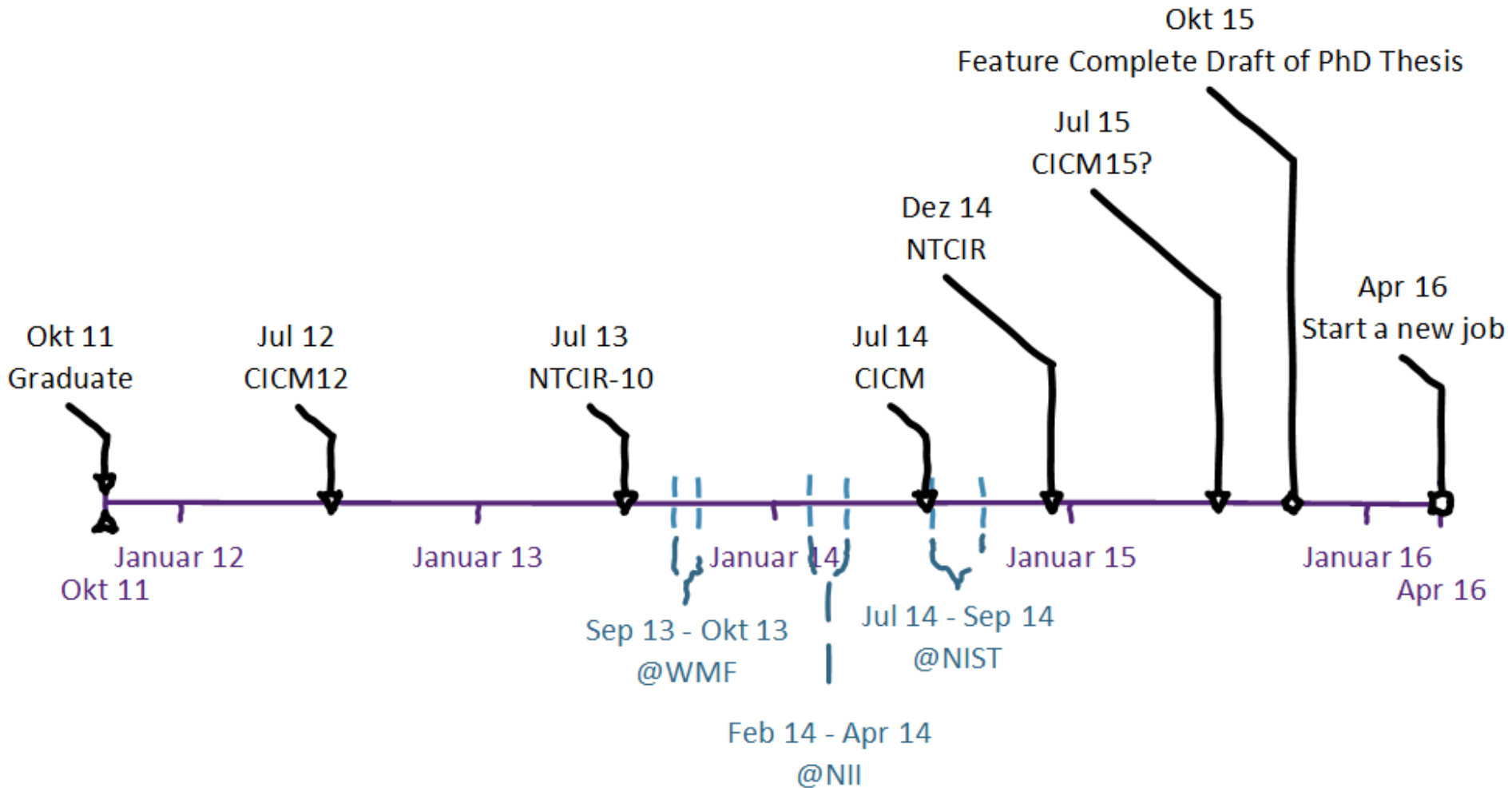


Overview





Time Table



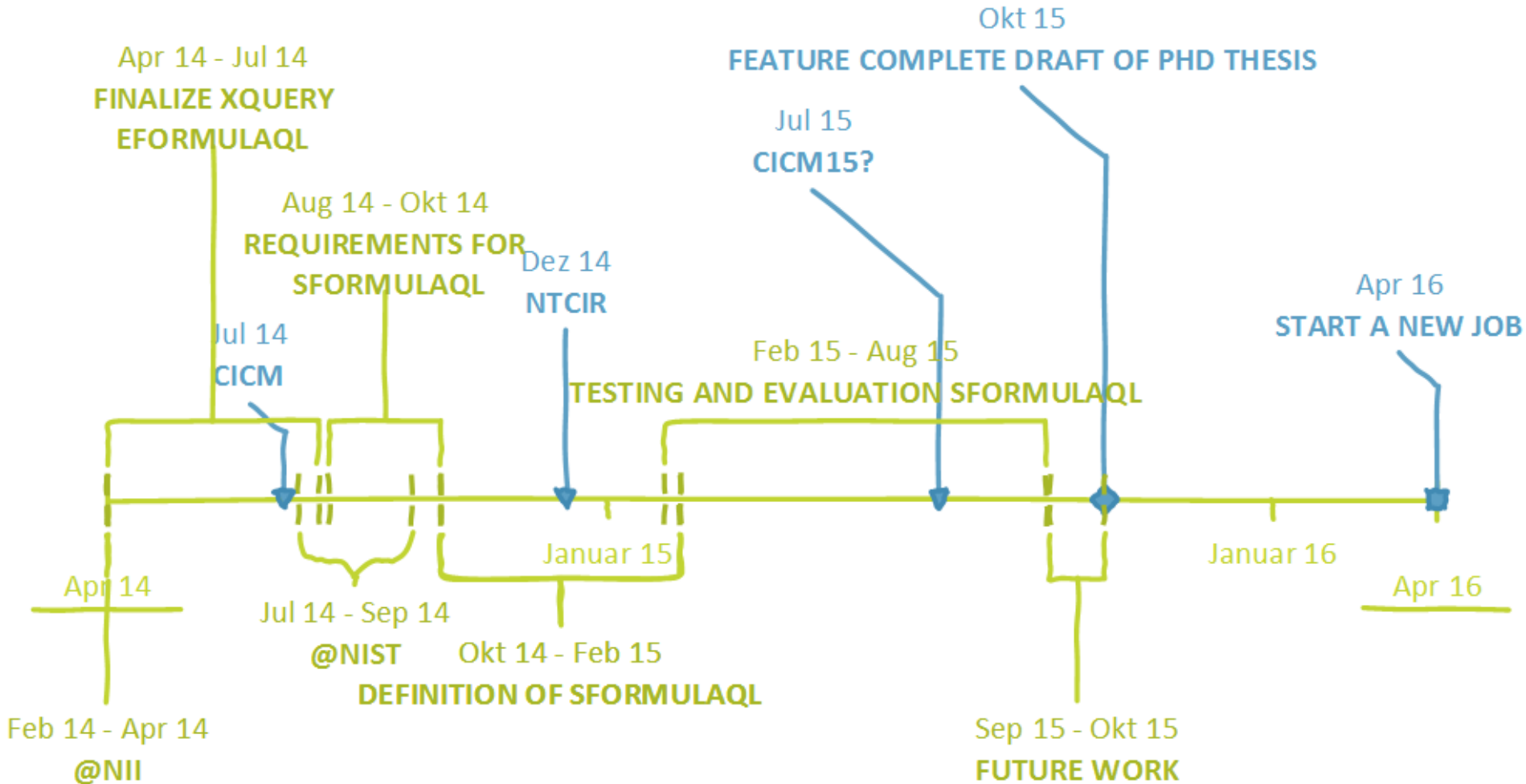


Completed Research

Querying	Processing	Scalability
<ul style="list-style-type: none">- Making Math Searchable in Wikipedia (CICM 2012)- Digital Repository of Mathematical Formulae (CICM 2014 coauthor)- Wikipedia Subtask at NTCIR 11 <div data-bbox="19 1053 595 1338"><p>Integrated Queries</p><p>Math Text Meta-data</p><p>Presentation Content Semantic Keywords Relations</p></div>	<ul style="list-style-type: none">- Mathematical Language Processing (submitted to CICM 2014)- Mathoid: Accessible Math Rendering for Wikipedia (submitted to CICM 2014) <div data-bbox="653 1213 1277 1320"></div>	<ul style="list-style-type: none">- qErrors in Multidimensional Histograms (2012)- Applying Stratosphere for Big Data Analytics (coauthor, BTW 2013)- Big Data Analytics for European Small and Medium-Sized Enterprises (European Dataforum 2013)- Querying large Collections of Mathematical Publications (NTCIR 2013 with Marcus Leich) <div data-bbox="1406 982 1866 1292"></div>



Future research

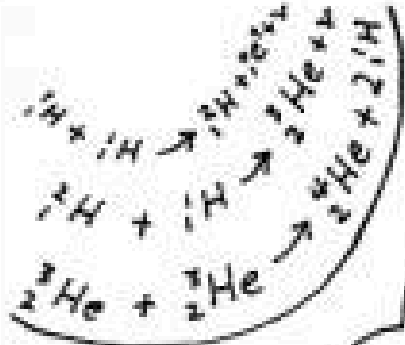




Excluded

- How scientists communicate with their colleagues? (user-study)
- Evaluation of the ease of use of query language (user-study)
- Measurement about the satisfaction of the scientist with the query results
- Guessing the users intention from the query
- Interface design for query input

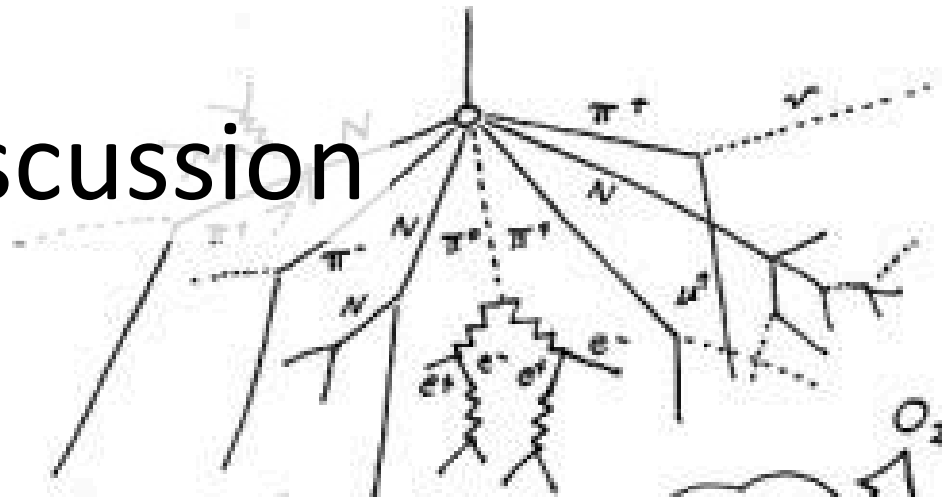
Discussion



$F = G \frac{m_1 m_2}{r^2}$

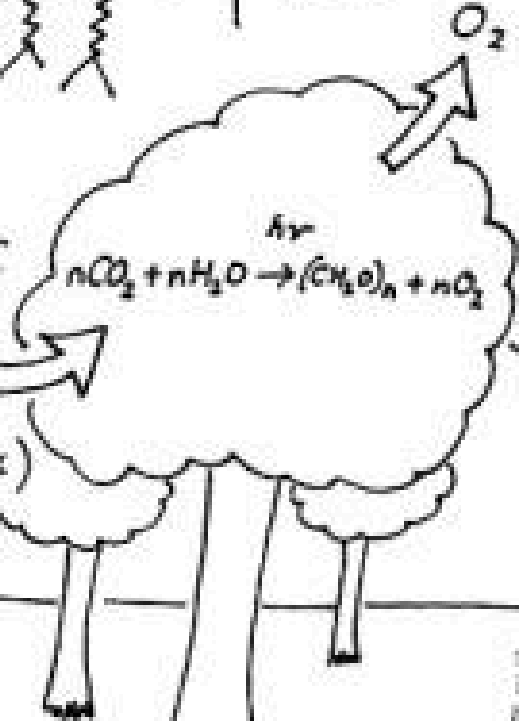
$R_{\text{univ}} = \frac{1}{2} R_{\text{grav}} = 8\pi G T_{\text{univ}}$

$\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0}$
 $\nabla \cdot \mathbf{B} = 0$
 $\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$
 $\nabla \times \mathbf{B} = \mu_0 \mathbf{j} + \mu_0 \epsilon_0 \frac{\partial \mathbf{E}}{\partial t}$



$P + \frac{1}{2} \rho v^2 + \rho g h = C$

$f(x) = a_0 + \sum_{n=1}^{\infty} (a_n \cos nx + b_n \sin nx)$



$\frac{\partial}{\partial t} \mu_i + \sum_{j=1}^N v_j \frac{\partial \mu_i}{\partial x_j} = \sum_{j=1}^N D_{ij} \frac{\partial^2 \mu_i}{\partial x_j^2}$

$\left[\frac{-\hbar^2}{2m} \nabla^2 + V \right] \Psi = i\hbar \frac{\partial}{\partial t} \Psi$



$f_1(x, y) = \begin{bmatrix} 0.85 & 0.87 \\ -0.84 & 0.85 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$
 $f_2(x, y) = \begin{bmatrix} 0.15 & \dots \\ 0.14 & \dots \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$